

COMPUTATIONS WITH XMVB@XACS

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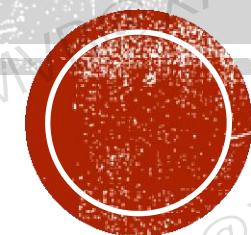
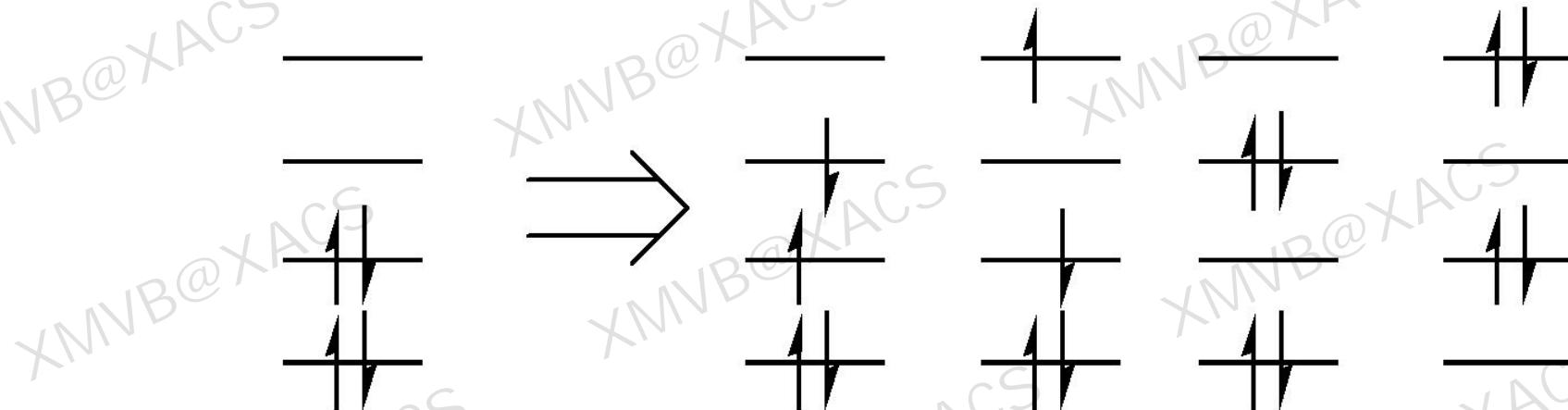


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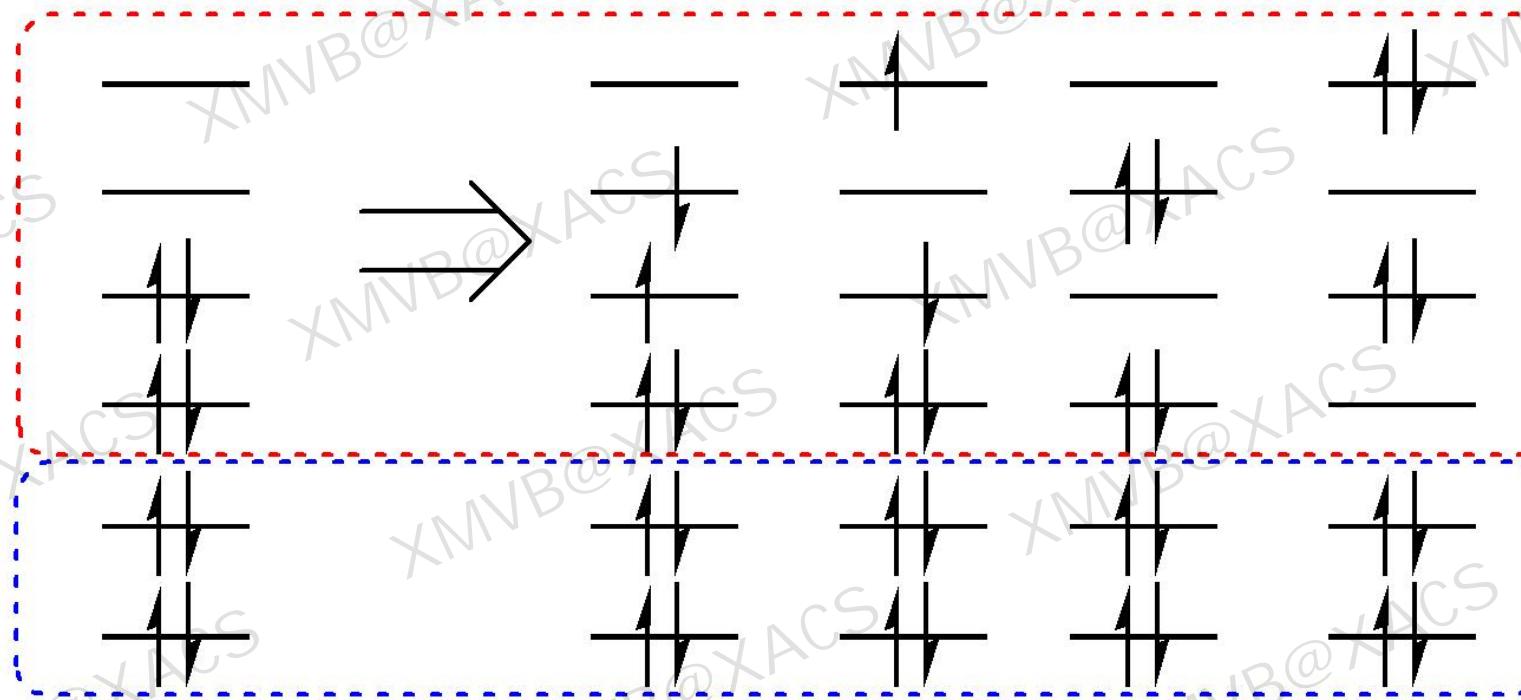
ACTIVE SPACE

- Multiconfigurational methods:
 - CASSCF/RASSCF
 - VB
 - ...
- Generating multiple determinants/configurations by excitations:



ACTIVE SPACE

- Spaces in Multiconfigurational wave function:
 - Inactive space**: orbitals are always doubly occupied
 - Active space**: orbitals are arbitrarily occupied



ACTIVE SPACE IN MULTICONFIGURATIONAL COMPUTATIONS

- 3 parameters to define an active space
 - Number of active electrons, m
 - Number of active orbitals, n
 - Multiplicity, S (same as multiplicity of the molecule)
- In VB computations, the interested bonds, unpaired electrons and corresponding orbitals ($S > 1$) should be included in the active space

ACTIVE SPACE: SOME EXAMPLES

- H_2
 - $m=2, n=2, S=1$ (H-H bond)
- O_2
 - $m=8, n=6, S=3$ (p_x, p_y and p_z orbitals)
- Benzene
 - $m=6, n=6, S=1$ (π orbitals)

H₂: BASIC CONCEPTS

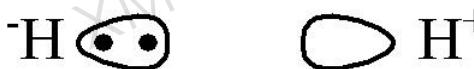
- The basic concepts of VB Theory:
 - Active space
 - VB structures and determinants
 - VB orbitals
- How to run VB computation:
 - Basic keywords
 - How to define active space
 - How to define VB orbitals
- Difference between DFT, CASSCF and VB

H_2 : BASIC CONCEPTS

- VB Structures



S_{cov}



$S_{\text{ion}1}$



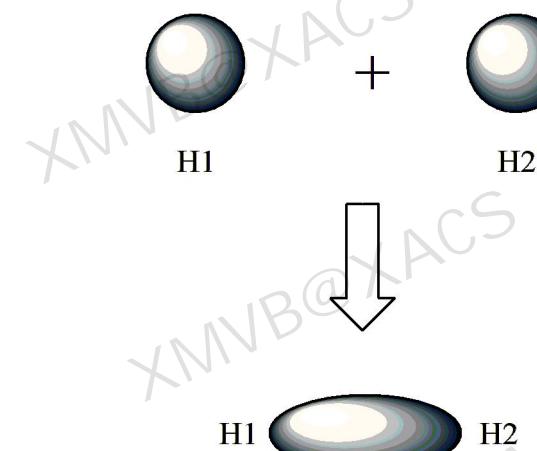
$S_{\text{ion}2}$

- VB Orbitals

- s orbitals on each H atoms

- Spaces

- No inactive space
 - Active space: $m=2$, $n=2$, $S=1$



H₂: BASIC CONCEPTS

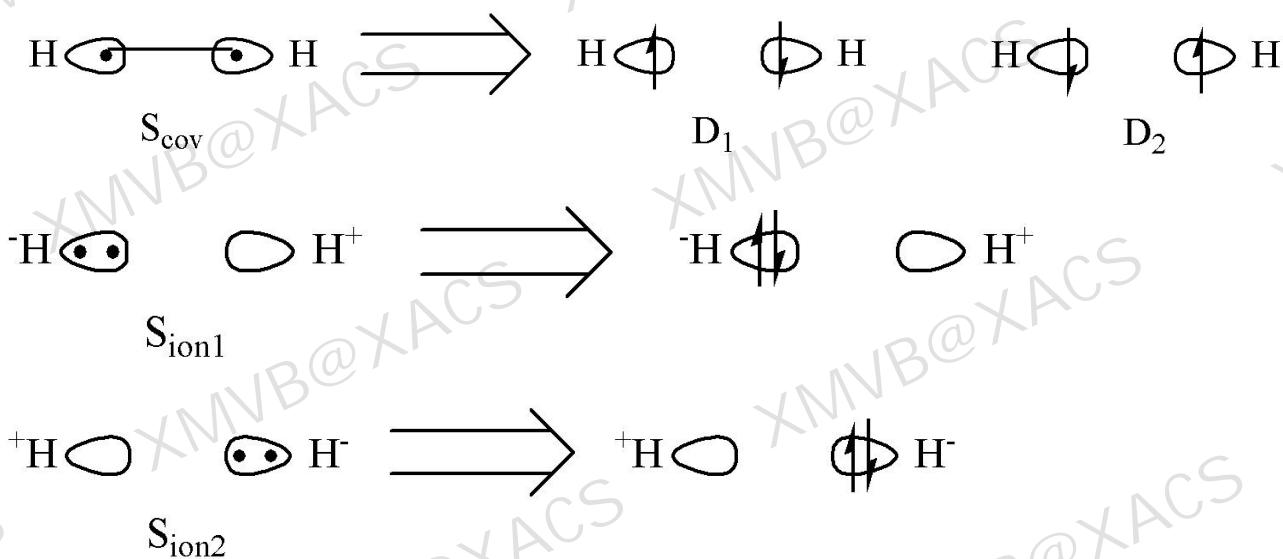
- **Wave Function**

$$\Phi_{cov} = \frac{1}{\sqrt{2 + 2S_{ab}}} (|\phi_a \bar{\phi}_b| - |\bar{\phi}_a \phi_b|)$$

$$\Phi_{ion1} = |\phi_a \bar{\phi}_a|$$

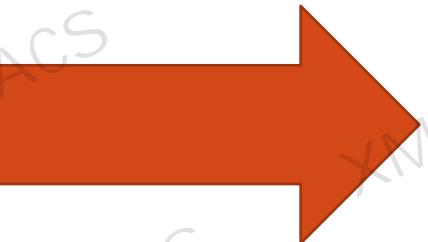
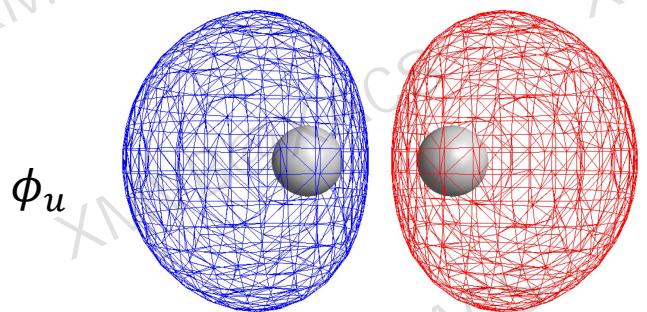
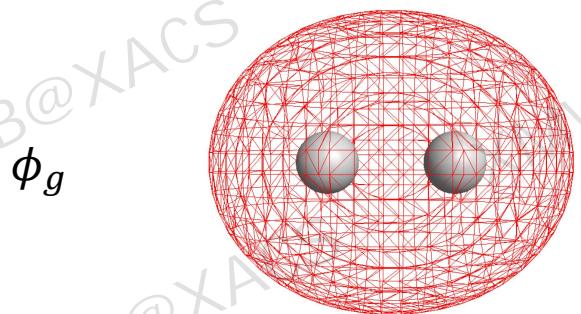
$$\Phi_{ion2} = |\phi_b \bar{\phi}_b|$$

$$\Psi = \sum_K C_K \Phi_K = C_{cov} \Phi_{cov} + C_{ion1} \Phi_{ion1} + C_{ion2} \Phi_{ion2} = C_{cov} \Phi_{cov} + C_{ion} (\Phi_{ion1} + \Phi_{ion2})$$

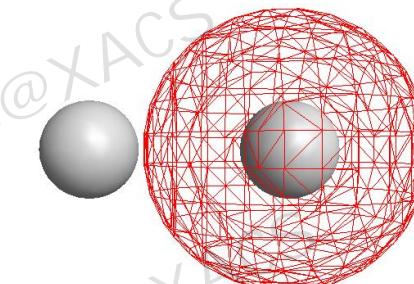
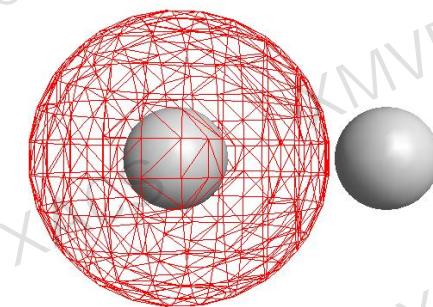


H₂: BASIC CONCEPTS

CASSCF Orbitals



VB Orbitals



H₂: BASIC CONCEPTS

Energies (in a.u.) of H₂ by various methods

Methods	Energy
HF	-1.128743
B3LYP	-1.166743
CASSCF	-1.147207
VBSCF	-1.146944

H₂: BASIC CONCEPTS

Coefficients by CASSCF

Configurations	Coefficients
$ \phi_g \bar{\phi}_g $	0.994
$ \phi_g \bar{\phi}_u - \bar{\phi}_g \phi_u $	0.000
$ \phi_u \bar{\phi}_u $	-0.110

Coefficients by VBSCF

Structure	Coefficients
S_{cov}	-0.835
S_{ion1}	-0.100
S_{ion2}	-0.100

F₂: BDE AND RESONANCE ENERGY

- Computations of bond dissociation energy (BDE) and resonance energy (RE)
 - How to compute BDE
 - How to compute RE
 - Definition of charge-shift (C-S) bond

F_2 : BDE AND RESONANCE ENERGY

- Bond Dissociation Energy (BDE):

$$E^{BDE} = E^\infty - E^{eq}$$

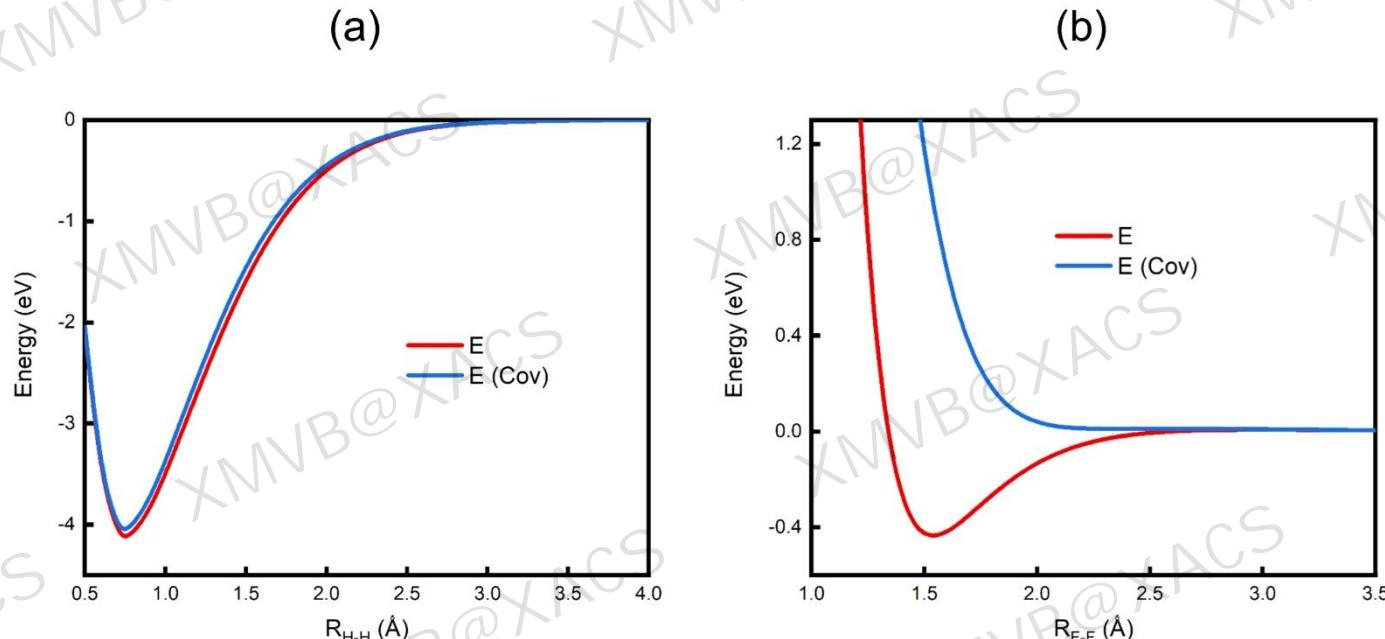
- Resonance Energy (RE):

$$E^{RE} = E^{FULL} - E^K$$

- Relative Resonance Energy (RRE):

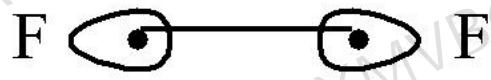
$$RRE = \frac{E^{RE}}{E^{BDE}} \times 100\%$$

RRE > 50% : Charge-Shift Bond

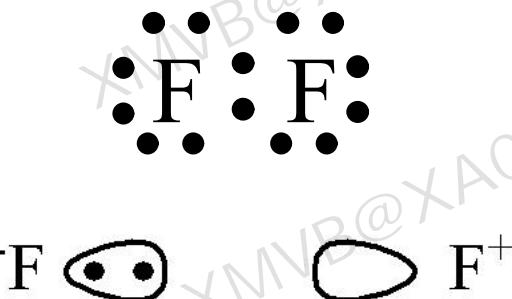


F_2 : BDE AND RESONANCE ENERGY

- VB Structures



S_{cov}



$S_{\text{ion}1}$



$S_{\text{ion}2}$

- Spaces:

- Inactive space: $m=16$ $n=8$ ($1s, 2s, 2p_x, 2p_y$)
- Active space: $m=2$ $n=2$ ($2p_z$)

F_2 : BDE AND RESONANCE ENERGY

Fragments

\$FRAG
1*6

- ① SPZDXXDYYDZZ 1 s, pz, dxx, etc on atom 1
- ② SPZDXXDYYDZZ 2
- ③ PXDXZ 1 ← px and dxz on atom 1
- ④ PXDXZ 2
- ⑤ PYDYZ 1 ← py and dyz on atom 1
- ⑥ PYDYZ 2
- \$END

6 fragments
1 atom in each

Orbitals

\$ORB
1*10

- ① 1
- ② 2
- ③ 1
- ④ 2
- ⑤ 3
- ⑥ 4
- ⑦ 5
- ⑧ 6
- ⑨ 1
- ⑩ 2

\$END

10 orbitals
1 fragment in each

fragment 1 in orbital 1

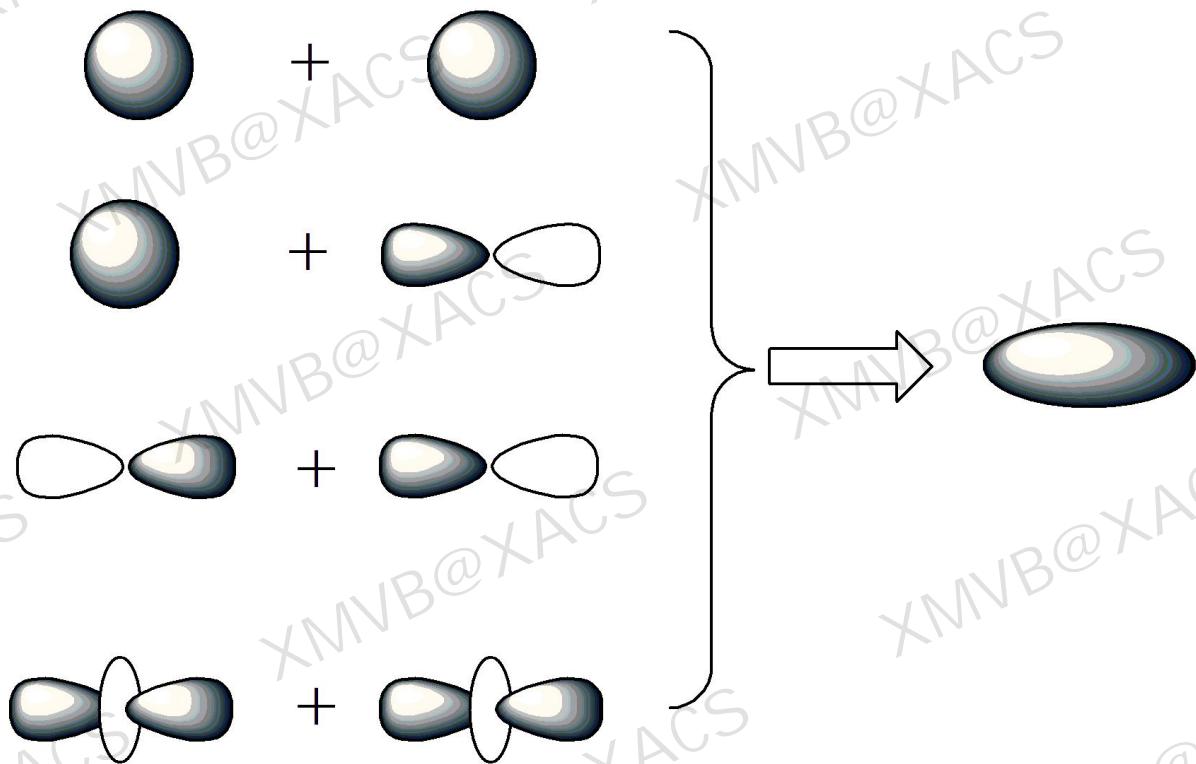
fragment 3 in orbital 5

Inactive space

Active space

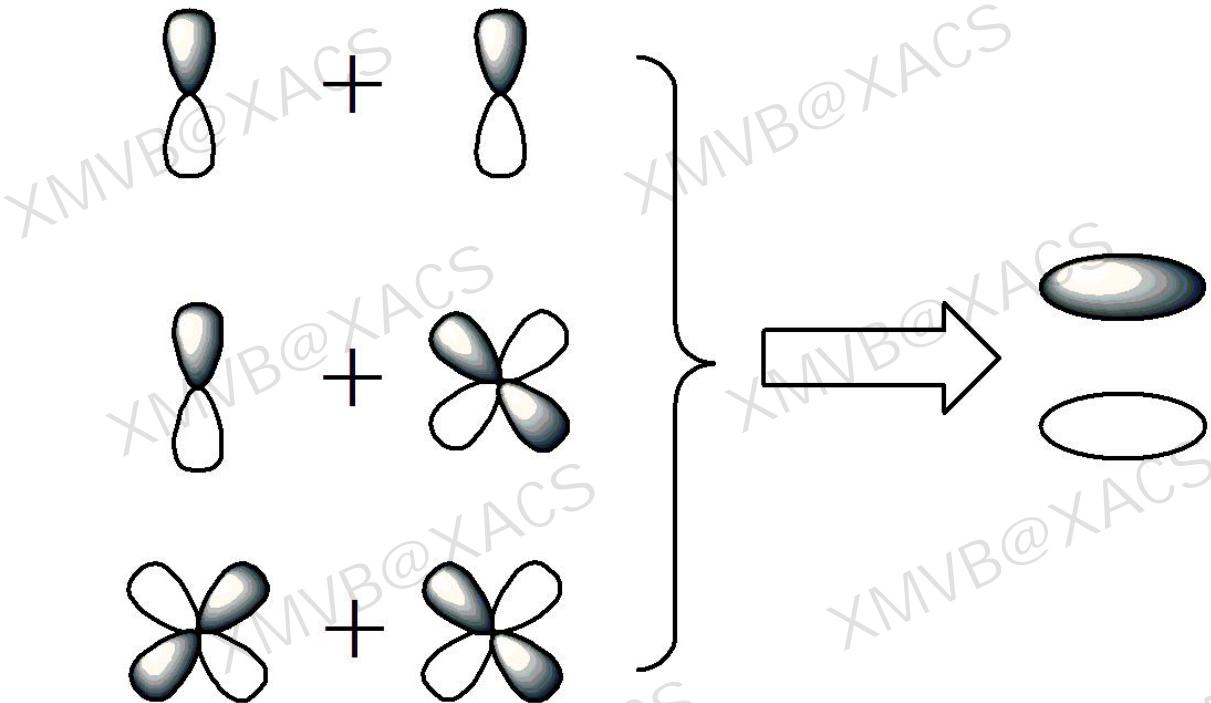
F_2 : BDE AND RESONANCE ENERGY

- σ Bonding in F_2

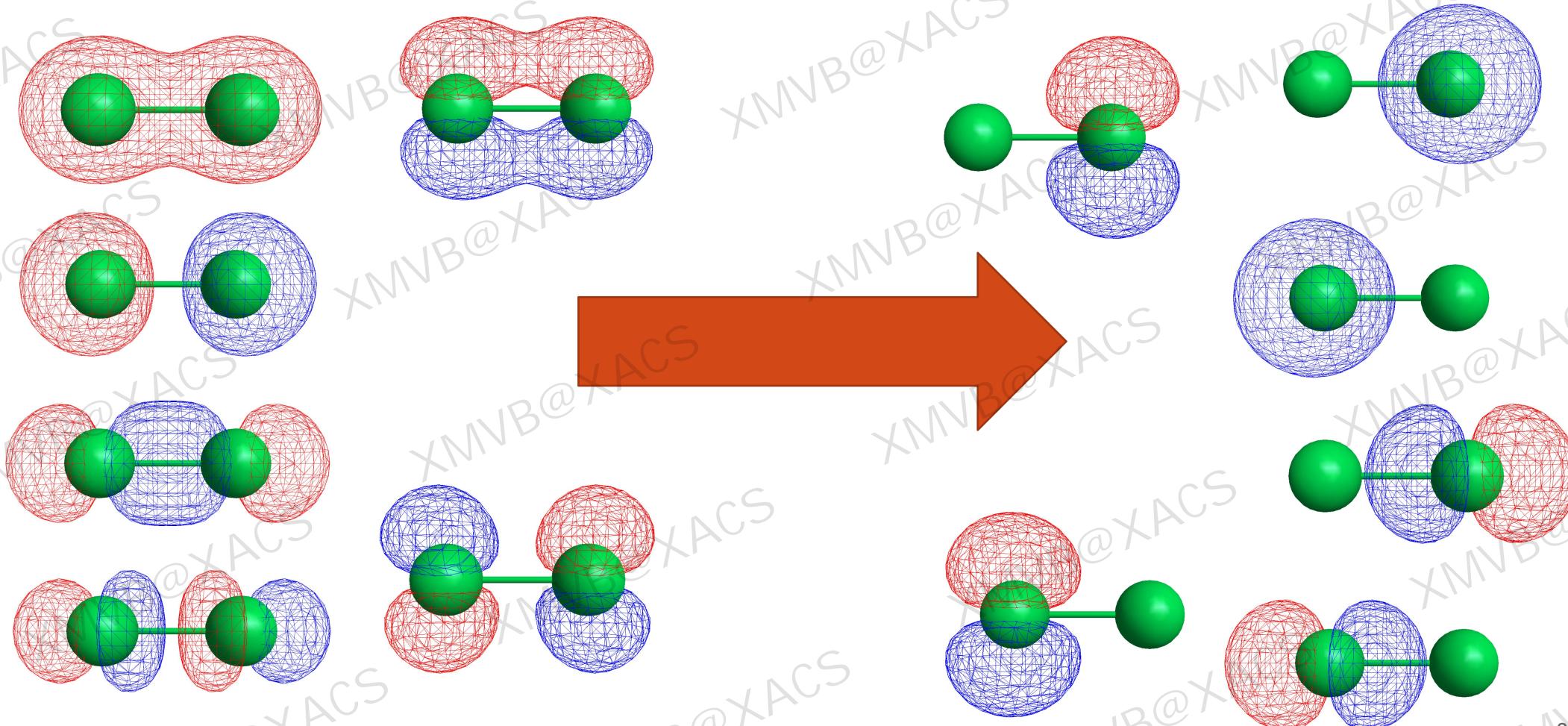


F_2 : BDE AND RESONANCE ENERGY

- π Bondings in F_2



F_2 : BDE AND RESONANCE ENERGY



F₂: BDE AND RESONANCE ENERGY

Energies and BDEs of F₂ by various methods

Methods	Energies (a .u.)		BDE (kcal/mol)
	Equilibrium	Dissociated	
HF	-198.687494	-198.743865	-35.4
B3LYP	-199.447478	-199.385090	39.1
CASSCF	-198.761112	-198.743865	10.8
VBSCF	-198.751156	-198.743865	4.6
BOVB	-198.783180	-198.743865	24.7
VBCISD	-198.972549	-198.930888	26.1
CCSD	-199.093045	-199.057382	22.4

ref: 38.2 kcal/mol

F₂: BDE AND RESONANCE ENERGY

REs and RREs of F₂ by VBSCF and VBCISD

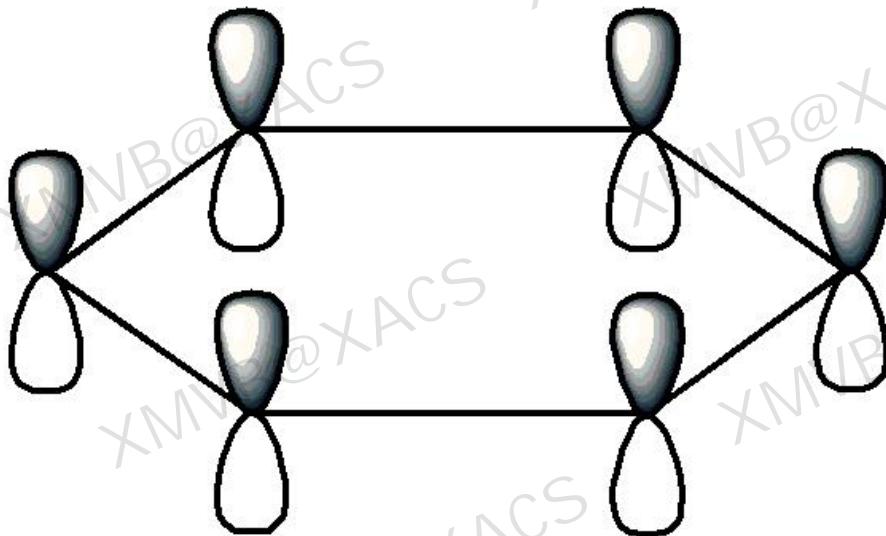
Methods	Energies (a .u.)		RE (kcal/mol)	BDE (kcal/mol)	RRE (%)
	Full	Cov			
VBSCF	-198.751156	-198.674860	47.9	4.6	1041.3
BOVB	-198.783180	-198.674860	68.0	24.7	275.0
VBCISD	-198.972549	-198.871326	63.5	26.1	243.3

C_6H_6 : RESONANCE AND AROMATICITY

- Purpose:
 - VB computation for molecules with conjugate π orbitals
 - The relationship between resonance and aromaticity

C_6H_6 : RESONANCE AND AROMATICITY

- Spaces:
 - Inactive: $m=36$ $n=18$ (all σ orbitals)
 - Active: $m=6$ $n=6$ (all π orbitals)

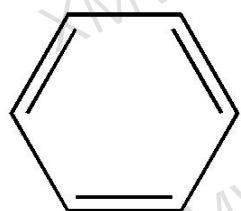


C_6H_6 : RESONANCE AND AROMATICITY

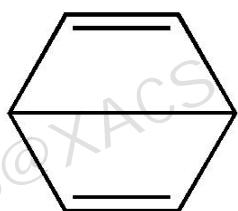
- Structures



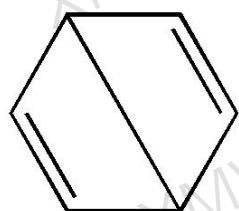
K1



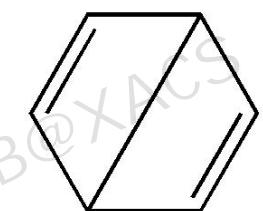
K2



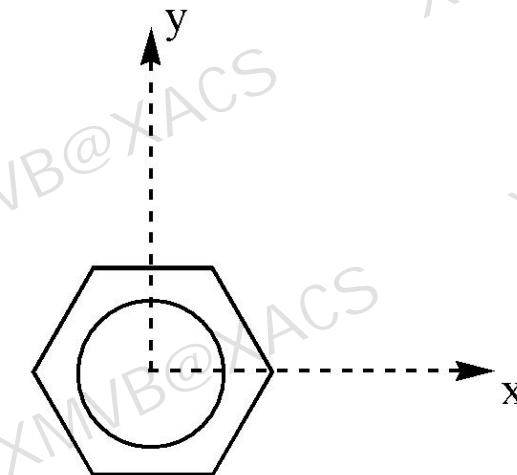
D1



D2

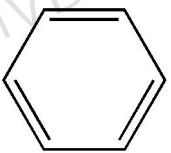


D3



C_6H_6 : RESONANCE AND AROMATICITY

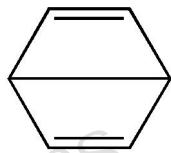
- Structures



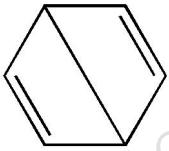
K1
19 20 21 22 23 24



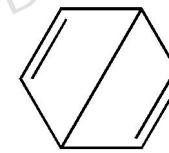
K2
20 21 22 23 19 24



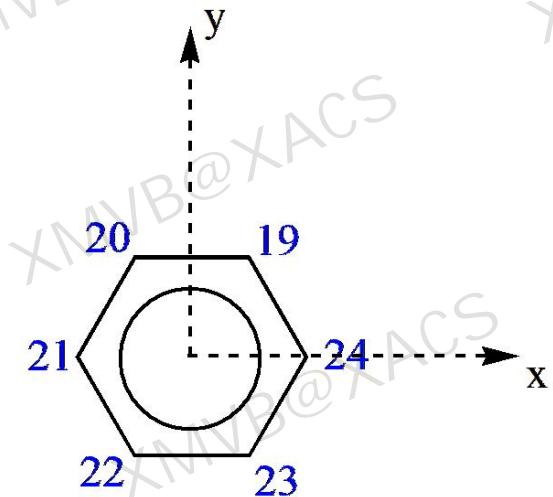
D1
19 20 22 23 21 24



D2
21 22 20 23 19 24



D3
20 21 19 22 23 24



C₆H₆ : RESONANCE AND AROMATICITY

- Results

Structure	Coef.	Weight
K1	-0.40080	0.333
K2	-0.40080	0.333
D1	0.14218	0.111
D2	0.14218	0.111
D3	0.14218	0.111

$$RE = E^K - E^{cov}$$

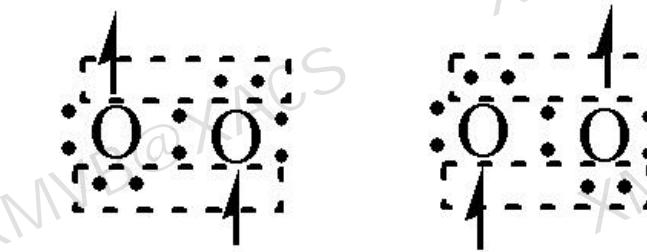
Computation	Energy (a.u.)	RE (kcal/mol)
5 Covalent Structures	-230.604424	--
2 Kekulé Structures	-230.599801	2.9
1 Kekulé Structure	-230.556432	30.1

O_2 : SINGLET AND TRIPLET

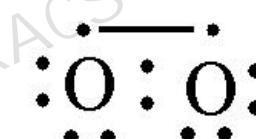
- Purposes:
 - VB computation for open-shell molecules
 - How to select structures
 - Computation for excited state

O_2 : SINGLET AND TRIPLET

- Singlet and Triplet States



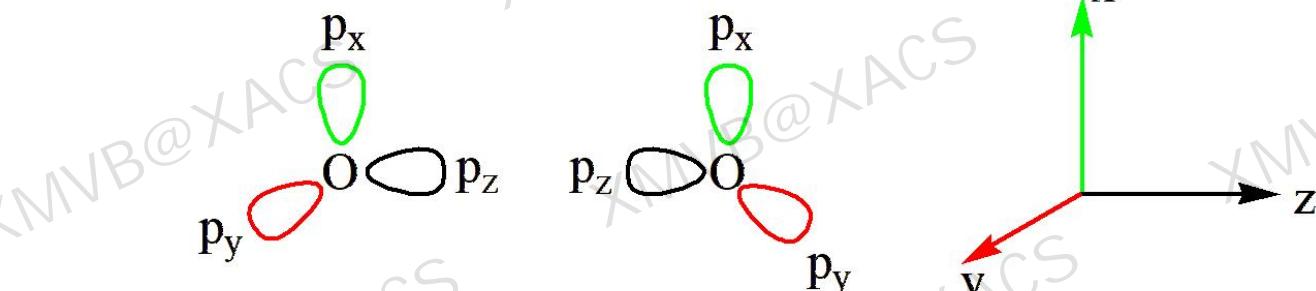
Triplet



Singlet

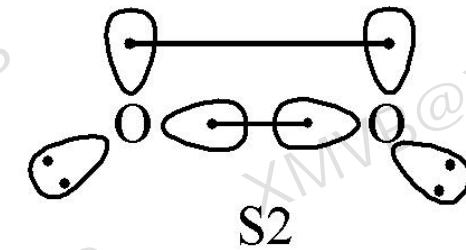
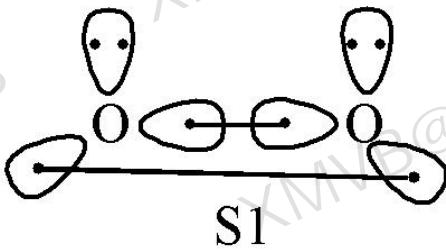
- Spaces:

- Inactive: $m=10$ $n=5$
- Active: $m=6$ $n=4$



O_2 : SINGLET AND TRIPLET

- Singlet Structures



- Triplet Structures

